

## $p$ -ADIC HODGE THEORY STUDY GROUP PLAN

- 1 (Lambert):** Overview of  $\ell$ -adic representations [3, Chapter 1]. Aim to understand definitions appearing in [1, Table I.3] (quasi-unipotent, unipotent, good reduction).
- 2 (Finn):** Motivation and Overview [2, I.1], [5, I.1], [1, I].
- 3 (James Timmins):** Étale  $\phi$ -modules ([2, I.3], especially Theorem 3.3.4; [3, Chapter 2], especially Theorem 2.33; [4, Chapter 2]).
- 4 (James Taylor):** Formalism of admissible representations ([2, I.5], especially Theorem 5.2.1; [5, III.1]).
- 5 (Arun):** Hodge-Tate representations and  $B_{\text{HT}}$  ([2, I.2], especially Theorem 2.4.11; [3, 5.1]).
- 6 (Rodrigo):** Perfectoid fields,  $A_{\text{inf}}$ , and  $B_{\text{dR}}$  (With perfectoid fields and  $A_{\text{inf}}$ : [5, III.2.1 - III.2.2], [4, 3-7]. Without perfectoid fields: [2, I.4], [5, II.2], [3, 5.2])
- 7 (George):** de-Rham representations ([2, II.6]; [5, III.2]; [3, Chapter 5])
- 8 (Lukas):** Isocrystals and filtered  $\phi$ -modules ([2, II. 7.3], motivated by  $p$ -divisible groups [2, II.7], especially Proposition 7.2.6). For a good introduction to  $p$ -divisible groups see [5, II].
- 9 (Hårvard):**  $(\phi, N)$ -modules ([2, II.8], especially Definition 8.2.5, Definition 8.2.9, and the paragraph directly before Section 8.3; [3, 6.4])
- 10 (Martin):** Crystalline representations and  $B_{\text{cris}}$  ([2, II.9]; [5, III.3]; [1, II.3]; [3, Chapter 6]; [4, 11,12]).
- 11 (-):** Semistable representations and  $B_{\text{st}}$  ([2, II.9]; [3, Chapter 6]; [1, II.3]). If time permits, an overview of all the period rings, with a comment on their topologies (a good starting point is [1, II.3.5]).
- 12 (Konstantin):**  $(\phi, \Gamma)$ -modules ([2, VI.13-VI.13], especially section III.13.6; [6] for a more detailed discussion, especially Theorem 3.3.10; [4, Chapter 3]; [3, 4.3, 4.4]).

Below the references are to the name of the corresponding file on the [shared folder](#).

### REFERENCES

- [1] Berger.
- [2] Brinon, Conrad.
- [3] Fontaine, Ouyang.
- [4] Gullota.
- [5] Hong.
- [6] Schneider.